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# A Key Generation technique using Concept of Recurrence Relation and Fuzzy logic against Security Breach in Wireless Communication

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**Abstract.** Wireless networking plays an important role in public and military applications. Security of information transfer through wireless networks remains a challenging issue. Wireless security is the process of designing, implementing, and ensuring security on a wireless computer network. Jamming and eavesdropping are two primary attacks at the physical layer of a wireless network. This article offers a study on the security vulnerabilities and threats on wireless communication and an efficient comprehensive mechanism for improving the wireless network security. In this paper, a stream cipher based symmetric key encryption with recurrence relation and fuzzy based session key has been proposed for wireless communication by satisfying the key issues like security; increase the strength of symmetric key. In this article we generate 'n' number of sub keys from symmetric key using XOR operation between a random character matrix and symmetric key. In this article the random numbers are generated by using recurrence relation which is a new approach in random number generation in discrete mathematics. Among these sub keys we generate a session key using fuzzy function. Now the encryption is done by using this session key and symmetric key. Here we transmit the session key to the recipient end by amalgamating with the symmetric key. This amalgamated form is send to recipient end for decryption. Here a new authentication scheme is used. Different types of randomness test have been done to test the randomness of our session key. The Brute-force attack analysis for this scheme and comparative study with existing standard methods has been done with satisfactory results.

**Keywords:** Wireless security, Symmetric key, Recurrence Relation, Random Character Matrix, Session key, Fuzzy logic, Encryption, Decryption.

## 1 Introduction

Wireless network have become a necessary part in our daily life. Now-a-days security is a vital issue in wireless application because wireless networks are heavily used for transmission of important or private information such as net banking service, e-shopping, bill payment etc. therefore, it is very important to share secret information reliably in the presence of eavesdroppers. Most commonly used security methods based on cryptographic technique are implemented at the upper layer of a wireless network. The existing physical layer security techniques can be classified into five major categories which are (i) theoretical secure capacity (ii) power (iii) code (iv)channel (v) signal detection approaches. In symmetric encryption or single-key encryption technique a common private key is shared by two users through a secure channel. Here physical layer method is employed to distribute secret keys to supply location privacy and to supplement upper layer security algorithms. It is very difficult for attacker to decipher transmitted information when physical security is applied.

**Table1.** Classification of security attacks in wireless communication

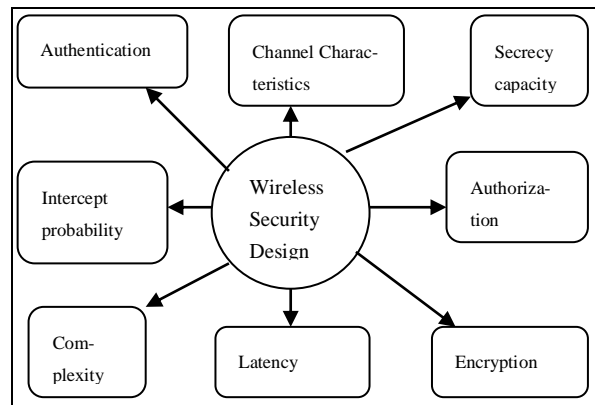
Passive Attacks	Active Attacks
Traffic Analysis	Denial of service attack
	Resource consumption
	Masquerade attack
Eavesdropping	Reply attack
	Information disclosure
	Message modification

In the following table summarizes the different types of attacks and different technologies against them with respect to basic security attributes.

**Table2.** Attack methods with security technologies

Computer Security Attributes	Attack Methods	Technology for Internet Security
Confidentiality	Eavesdropping, Hacking, IP spoofing, phishing, DoS.	IDS, firewall, cryptographic system, IPSec, SSL
Integrity	Viruses, Worms, Trojans, Eavesdropping, Hacking, IP spoofing, phishing, DoS.	IDS, firewall, anti-malware s/w, IPSec, SSL
Privacy	E-mail bombing, Spamming, Cookies, IP spoofing.	IDS, firewall, anti-malware s/w, IPSec, SSL
Availability	E-mail bombing, Spamming, Cookies, IP spoofing, System boot record interface.	IDS, firewall, anti-malware s/w

In this article, we have given stream cipher based symmetric key encryption with session key to try to ensure security at physical layer in wireless network.



**Fig1.** Wireless security methodology and design factor.

A symmetric encryption scheme has five parts- i) plaintext ii) encryption algorithm iii) secret key iv) cipher text iv) decryption algorithm [1], [3].

For secure use of symmetric encryption, we should focus on two requirements-

i) Strong encryption algorithm ii) secret key, sender and receiver must have the copies of this key in a secure fashion. The two basic building block of all encryption algorithms are substitution and transposition. There are two types of algorithms stream cipher and block cipher and four types of algorithm modes Electronic Code Book (ECB), Cipher Block Chaining (CBC), Cipher feedback (CFB), Output Feedback (OFB). Many Symmetric encryption algorithms are: Data Encryption Standard (DES), Triple DES (3DES), International Data Encryption algorithm (IDEA), Blowfish, Advanced Encryption Standard (AES). Symmetric key algorithm is also known as private key algorithm.

DES: - Data Encryption Standard [2] uses block cipher structure. It encrypts data in blocks of size 64 bits each. 64 bits of plain text is treated as the input to DES, which produces 64 bits of cipher text. Initially the key length is 64 bits. Before starting of DES process every eight bit of the key is discarded to produce a 56-bit key. DES based on two main concept of cryptography: confusion and diffusion. DES consists of 16 rounds and each round performs the step of substitution and transposition. DES results in a permutation among the  $2^{64}$  possible arrangements of 64 bits, each of which may be either 0 or 1.

DOUBLE DES: - Double Data Encryption Standard [2], [3] is simple to understand and it performs twice what DES does only once. Double DES uses two keys say, key1 and key2. It first performs as DES on the original plain text using key1 to get the encrypted text. It again performs as DES on the encrypted text by using the other key (that is, key2). The final output is the encryption of the encrypted text. Now for decryption, the doubly encrypted cipher text block is first decrypted using the first key (key2) to produce first round encrypted cipher text. This cipher text block is then decrypted using the key (key1) to obtain the original plain text.

RC5:- RC5 [2], [3] is a symmetric key block encryption algorithm developed by Ron Rivest. The main theme of RC5 is that it is fast because it uses only the primitive operations (XOR, Shift etc). It allows for a variable number of rounds and a variable bit-size key to add to the flexibility. RC5 uses less memory for execution. In RC5, the word size, number of rounds, number of octets of the key, all may be variable length but those values remain same for a particular execution of the cryptographic algorithm. The output of RC5 is the cipher text which is same size as the input plain text.

RECURRENCE RELATION IN RANDOM NUMBER GENERATION: - Each term of a sequence is a linear function of earlier terms in the sequence is linear recurrence. Recurrence relation is of two types- 1) linear recurrence relation 2) linear non homogeneous recurrence relation [21].

- 1) Linear recurrence relation:- A linear homogenous recurrence relation of degree k with Constant coefficients is a recurrence relation of the form

$$a_n = c_1 a_{n-1} + c_2 a_{n-2} + \dots + c_k a_{n-k}, \text{ where } c_1, c_2, \dots, c_k \text{ are real numbers, and } c_k \neq 0. \\ a_n \text{ is expressed in terms of the previous k terms of the sequence.}$$

Proposition: Let  $a_n = c_1 a_{n-1} + c_2 a_{n-2} + \dots + c_k a_{n-k}$  be a linear homogeneous recurrence.

- Assume the sequence  $a_n$  satisfies the recurrence.
- Assume the sequence  $a'_n$  also satisfies the recurrence.
- So,  $b_n = a_n + a'_n$  and  $d_n = \alpha a_n$  are also sequences that satisfy the recurrence. ( $\alpha$  is any constant).

- 2) Linear non-homogeneous recurrence: - A linear non-homogenous recurrence relation with constant coefficients is a recurrence relation of the form

$$a_n = c_1 a_{n-1} + c_2 a_{n-2} + \dots + c_k a_{n-k} + f(n), \text{ where } c_1, c_2, \dots, c_k \text{ are real numbers, and } \\ f(n) \text{ is a function depending only on n. The recurrence relation } a_n = c_1 a_{n-1} + c_2 a_{n-2} + \\ \dots + c_k a_{n-k}, \text{ is called the associated homogeneous recurrence relation.}$$

Proposition:

- Let  $a_n = c_1 a_{n-1} + c_2 a_{n-2} + \dots + c_k a_{n-k} + f(n)$  be a linear non-homogeneous recurrence.

- Assume the sequence  $b_n$  satisfies the recurrence.
- Another sequence  $a_n$  satisfies the non homogeneous recurrence if and only if  $h_n = a_n - b_n$  is also a sequence that satisfies the associated homogeneous recurrence.

In our article we use linear non homogeneous recurrence relation for generating random numbers. This is another concept to generate random numbers without using `rand()`. Any recurrence relation can be used in random number generation. For example here we use the recurrence  $a[i] = c[0] * a[i - 1] + c[1] * a[i - 2] + c[2] * a[i - 3] + \dots + c[m] * a[i - m + 1] + pow(2, i)$ . The initial condition and coefficient values are given at first, according to these conditions and values the random numbers are generated.

**PSEUDORANDOM FUNCTION (PRF):** - A PRF is used to produce a pseudorandom string of bits of some fixed length. The PRF takes as input a seed and some context specific values. In our technique strings of bits are not fixed and dependent on user that is the total number of random numbers is chosen by user as well as context specific values also. Here recurrence relation formula is used in PRF [3].

**FUZZY LOGIC:** - Fuzzy logic [4], [5], [6], [7] deals with fuzzy predicates and fuzzy implications made up of fuzzy predicates. It also deals with how to make inferences using fuzzy predicates and fuzzy implications. A fuzzy predicate is described in terms of fuzzy sets and a fuzzy implication is described in terms of fuzzy relations. Fuzzy relations are special kind of fuzzy sets whose domains are Cartesian products of domain. It is also needed in the compositional form of reasoning. Fuzzy sets were introduced by Prof. Lotfi A. Zadeh of University of California at Berkeley [7]. A fuzzy set on a universal domain  $U$  is defined by its membership function from  $U$  to  $[0, 1]$ . Thus by a fuzzy set on  $U$  is meant a function  $A: U \rightarrow [0, 1]$ . 'A' is called the membership function,  $A(x)$  is called the membership grade of  $x$ . we can write  $A = \{x, A(x): x \in U\}$ . It deals with reasoning with inexact or fuzzy concept. The fuzzy logic encompasses the fuzzy relations and fuzzy sets and  $[0, 1]$  is its truth value set. Most of the fuzzy logic is based on the following definitions for the logical connectives,  $\vee$ , and  $\wedge$ .

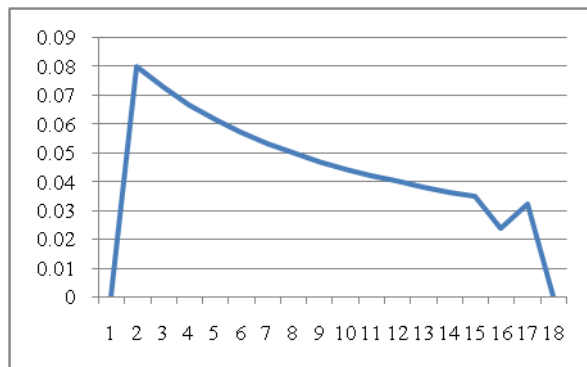
$$T(p \vee q) = \max[T(p), T(q)], T(p \wedge q) = \min[T(p), T(q)], T(\sim p) = 1 - T(p).$$

**Fuzzy Membership Functions:** - All information contained in a fuzzy set is described by its membership function. The features of this function are given below.

The *core* of a membership function for some fuzzy set  $A_{\sim}$  is defined as a region of the universe which is characterized by complete and full membership in the  $A_{\sim}$ . So, the core comprises those elements  $x$  of the universe such that  $\mu_{A_{\sim}}(x) = 1$ .

The *support* of a membership function for some fuzzy set  $A_{\sim}$  is defined as a region of the universe that is characterized by nonzero membership in the  $A_{\sim}$ . So, the support comprises those elements  $x$  of the universe such that  $\mu_{A_{\sim}}^{(x)} > 0$ .

The *boundaries* of a membership function for some fuzzy set  $A_{\sim}$  are defined as a region of the universe containing elements that have a nonzero membership but not complete membership. That is, the boundaries comprise those elements  $x$  of the universe such that  $0 < \mu_{A_{\sim}}^{(x)} < 1$ . These elements of the universe are those with some *degree* of fuzziness, or only partial membership in the fuzzy set  $A_{\sim}$ . In our scheme, fuzzy concept is used to generate session key. The membership function is chosen based on intuitive understanding of the problem definition [4], [5], [6]. Here we deduce the following function  $f(x) = (\text{half the size of the symmetric key}/\text{total ascii bit diff}(x))$ ,  $90 < x \leq 255$ . This proposed function satisfies all the features of membership function. A diagram is given below to represent the characteristics of our fuzzy membership function.



**Fig2.** Characteristics of fuzzy membership function

### 1.1 RELATED WORK:-

Now-a-days the data Security has become a serious matter with the progress of communication technology. In the symmetric key encryption, DES was adopted as national standard in 1976. Besides DES, two variations of DES have emerged which are double DES and triple DES where two keys and three keys are used to increase the robustness of encryption. IDEA [3], RC4, RC5, BLOWFISH, TWOFISH [3] are different types of symmetric key encryption algorithm. National Institute of Standards and Technology (NIST) announced the Advanced Encryption Standard (AES), in 2001. AES algorithm is a symmetric block cipher with low complexity and high security level. NIST also proposed Secure Hash Algorithm (SHA) for authentication. When new encryption technique is introduced, cryptanalysts starts to develop to attack. Eli Biham and Adi Shamir introduced the concept of differential cryptanalysis [8]. This method looks at pairs of cipher text whose plain texts have particular differences. Mitsuru Matsui invented the linear cryptanalysis attack [10] based on linear approximation. Timing attack is also applied on symmetric key encryption. There also exists Sensor Network Encryption Protocol (SNEP) [2] for security of sensor network systems. Chanchala Joshi and Umesh Kumar Singh [17] focuses on information security risk assessment, prioritizes the information assets and identification and monitoring of specific threats. This also suggests a conceptual framework of info-structure of ISRA. Thus many encryption algorithms are widely available and used in information security and also different types of attacks are available to break the security. In Symmetric keys (or private key) encryption or secret key encryption, only one key is used to encrypt and decrypt data. DES uses one 56-bits key. Double DES uses two 56 bits key and Triple DES (3DES) uses three 56- bits keys. While AES uses various (128,192,256) bits keys. At present different types concepts, logic like fuzzy logic, neural network etc. also introduced in cryptography for increasing the robustness encryption. Our paper proposed a technique called FSKRPSKE which provides a fuzzy based session key from symmetric key using a random character key matrix. Here session key is generated using fuzzy logic. Using these two keys we can encrypt a file (.txt, .doc, etc) and by the reverse way we can decrypt the cipher text to get plain text.

### 1.2 PRESENT PROBLEM SCENARIOS IN WIRELES COMMUNICATIONS:-

In wireless network, the data and information are exchanged among different authorized users, but this process is vulnerable to various bitchy threats. Hence, it is paramount importance to improve wireless communication security to fight against different types of attacks like eavesdropping DoS, cyber-criminal activities. The main wireless security methodologies include the authentication, authorization and encryption. Cryptography is used for encryption process and also it improves the achievable communication confidentiality. But it requires additional computational power and robustness in encryption and decryption process. In symmetric key encryption we can transmit huge amount of data between sender and receiver effectively through wireless communication. But the whole encryption is done using a private key (symmetric key). If this private key is revealed by attackers then overall communication is under threat. Existing symmetric key encryption algorithm does not change their key/keys with respect to

time. So the use of a single fixed key or multiple fixed keys is a problem in encryption process. Thus security in wireless communication is very necessary because of its more and more use in Smartphone, online banking, e-shopping etc.

### 1.3 SOLUTION DOMAIN & OBJECTIVES:-

In this paper we are motivated to discuss diverse wireless attacks and the corresponding defense mechanisms. Wireless networks generally adopt the OSI protocol architecture. The security threats and vulnerabilities associated with the OSI protocol are protected separately at each layer to meet the security requirements like authenticity, confidentiality, integrity and availability. Different types of cryptographic techniques are widely used to protect threats and attacks in wireless communication. In this article our objective is to propose a cryptographic technique which provides confidentiality and authenticity. The technique is mainly divides into three phases; key generation phase, encryption phase, authentication phase and decryption phase. In key generation phase, we generate an extra key called session key [4] from the symmetric key by using a random character matrix, fuzzy logic. Since this session key may change time to time so the use of both session key and symmetric key and CLS operation in encryption provides the extra robustness in our technique. Here we deduce a novel technique for authentication proof by using both the symmetric key and session key. Thus, the use of session key with symmetric key and an authentication cum encryption provides the added flavor and beauty in our proposed technique.

## 2 METHODOLOGY

Our proposed technique is composed of four parts which are (i) Session key generation (ii) Encryption with symmetric key and session key (iii) Authentication check and session key transpired. iv) Decryption. For session key generation to crate random numbers we use the formula for non homogeneous recurrence relation. The summary of our scheme is described by a compact algorithm, given below.

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#### ALGORITHM:

Input: - plain text, symmetric key.

Output: - encrypted file with header and tailer.

---

Method: -

1. Call RCG ( ) // Random character generation using non homogeneous recurrence relation
  2. Call MGA ( ) // matrix is generated to create 'n' number of key population from symmetric key.
  3. Call SKG ( ) // generate session key using 'n' number of key populations and fuzzy logic.
  4. Call EP ( ) // Encryption Process i.e., cipher file is generated using two keys.
  5. Call Create\_Header\_Tailer ( ) // header and tailer structure is created using two keys with XOR operation.
  6. Call Concate(header, encrypted file, tailer) // total structure is created and it is ready for transmission over network.
  7. Call AuthenticationCheck ( ) // check authentication using two keys and also generate session key using symmetric key.
  8. Call DrypPhase ( ) // plain text is generated.
- 

All the above methods in the algorithm are described below in details.

#### SESSION KEY GENERATION PHASE:

The session key generation process is divided into two parts. First is pre defined matrix generation and second is session key generation from symmetric key using fuzzy logic.

In the first part the predefined matrix is a square matrix with random characters, this random characters are generated using non homogeneous recurrence relation. A details algorithm is given below for random

character generation. The number of column of matrix is half of the size of the symmetric key. If the key size is 'n' byte then no. of row and column of matrix is n/2.

**ALGORITHM-1: Random Character Generation using Non-Homogeneous Recurrence Relation (RCG)**

Input: seed value, coefficient value and non homogeneous recurrence equation.

Output: random character value.

Method:

```

1. Set i, j, m, n, f, lr as integer and a[m], r[n], c[m] as integer array.
2. n<- total random number
3. m<- total no. of coefficient in non-homogeneous recurrence relation.
4. For i=0 to m
5. c[i]<- get_coeff()
6. a[i]<-get_seedVal()
   end for
7. lr<- get_largestPrimeFact(a[2] xor c[3]).
   {/* a[2] and c [3] are chosen by the user.*/}
8. a[0]<- a[0] xor lr.
9. for i=1 to m
10. a[i]=(a[i]xor a[i-1])xor lr
   end for
11. for i=3 to n
12. a[i]<-get_val(rec_Funct(i))
13. if(a[i]<0)
14. a[i]<- -a[i]
   end if
15. r[i]<-a[i]
16. f<-(((a[i]xor c[1])xor c[3])xor c[5])xor...c[m])
17. a[i]<-f
   end for
18. if(n>=3)
   r[n]<-get_shuffle(r[n])
   end if
19: End

```

**ALGORITHM-2: Matrix Generation Algorithm (MGA)**

Input: - randarr[m]: character array.

Output: - a square matrix (kmatrix[m][m]).

Method: -

```

1. Set m, i and j as integer.
2. m= half(symmetric key size).
3. kmatrix[m][m]={0}
4. for i=0 to m
5. randarr[i]= get_randomchar();
6. end for
7. for i=0 to m
8. for j=0 to m
9. kmatrix [i][j]=randarr[j]
10. end for
11. randarr[i]←rightShft(randarr[i])
12. end for
13. End.

```





After encryption with two keys we create a format with Header, cipher text and Tailer [13] using the function *Concat()*. The result of this function is the compact form of text which is ready for transmission to the receiver end. We use Tailer part to check authentication and Header part for session key generation in recipient end. Now the Header and Tailer structure is created using the following algorithm.

HEADER AND TAILER CREATION: -

ALGORITHM-4: *Create\_Header\_Tailer ()*

Input: - symmetric key, session key (SK[m]).

Output: - Header and Tailer.

Method: -

1. Set  $F\_half$ ,  $L\_half$  and  $diagEl$  as character arrays.
2. Set  $key\_Mat$   $[][]$  as 2D character array.
3.  $F\_half \leftarrow$  first half of symmetric key, and  $L\_half \leftarrow$  last\_half of symmetric key.
4. set  $m =$  ascii valueOf(1<sup>st</sup> character of symmetric key)
5.  $Header \leftarrow ((keyarr [] \text{ XOR } L\_half)) \ll (m \text{ mod length (symmetricKey)})$ .
6.  $Key\_Mat \leftarrow$  Call *create\_matrix* ( $F\_half$ , session key)
7.  $ColmnEl \leftarrow$  *get\_2ndColmn* ( $key\_Mat$ )
8.  $Tailer \leftarrow$  *bit\_XOROP* ( $ColmnEl$ ,  $L\_half$ ) //  $diagEl$  is XORed with  $L\_half$ , bit by bit up to the last bit of  $L\_half$ .
9. End

If symmetric key is 16 byte the session key is 8 byte and the total structure is given below which is created by calling the function *Concat ()* which is given in main algorithm.

Header (8byte)	Encrypted file	Tailer (8 byte)
----------------	----------------	-----------------

DECRYPTION PHASE:

The decryption phase is occurred in recipient end, first of all, Header section, encrypted file and Tailer section are separated using the symmetric key. Here we call *Create\_Header\_Tailer ()* function so that we can reveal the session key using the symmetric key from Header section and we can check the authentication from Tailer part using the function *AuthenticationCheck()*. If authentication phase shows green signal then plain text is generated from encrypted file using both session key and symmetric key in reverse process of encryption phase.

SIGNIFICANCE OF AUTHENTICATION: - Authentication mechanisms [8] provide the proof of identities. The authentication process ensures that the origin of document is correctly identified i.e, the document is coming from right user. In our scheme we use authentication part for proof of identities. We know that symmetric key encryption provides authentication and confidentiality. But we are qualified this statement using an extra authentication scheme in our proposed technique. Here we use two structures of Header and Tailer. There are complex calculations for Header and Tailer generation. Tailer structure is used for authentication check. In receiver side symmetric key and particular row are used to generate session key. Now using this session key and symmetric key we check identities of user from Tailer part. Thus our technique protects the fabrication.

### 3 Results and Discussions

**Table3.** Specifications of H/w and S/w used in the experiment

<b>Computer</b>	Lenovo G80.
<b>Processor</b>	Intel® Pentium® CPU B950@210GHz
<b>RAM</b>	2GB
<b>Compiler</b>	Turbo C
<b>Disc Drive</b>	SA 9500325AS ATA
<b>Operating System</b>	Windows 7 Ultimate (32 Bits)

In this section, simulation results of the proposed technique are presented. All the programs and calculations are done in a machine with above configuration. In our experiments, several sizes of different types of files are used as plain text.

Our result section is divided into four parts: (i) Attacks Analysis (ii) Randomness test & Entropy test of session key (iii) Analysis of encryption technique and (iv) Comparisons among standard algorithms and some other techniques.

#### DIFFERENT TYPES OF ATTACKS ANALYSIS: -

There are different types of attacks are exists to recover the key in use rather than simply to recover the plain text. There are two general approaches are – (i) Brute-force attack [11], [12] (ii) Cryptanalysis (Dictionary Attack) [22].

#### KEY SPACE ANALYSIS

The size of key space is the total number of different keys in encryption process. The brute-force attack is impractical in such crypto systems where key space is large. Now we consider a general case where secret key is  $x$  bits. There are two keys are in our proposed technique, first is symmetric key with size  $x$  bits and second is session key whose size is  $x/2$  bits. Now for the symmetric key, the key space is  $2^x$  and for session key, the key space is  $2^{x/2}$  and total key space is  $2^{3x/2}$ . Using this large key space we discuss following things.

#### BRUTE-FORCE ATTACK:-

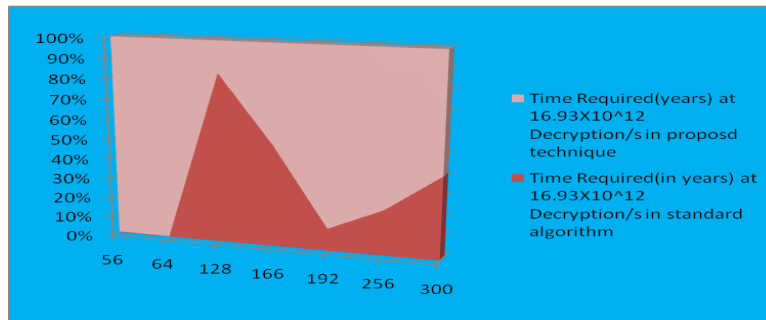
A good encryption technique satisfies the requirements of resisting brute-force attack. In this attack, attacker tries to translate the cipher text into plain text using every possible key. On average, half of all possible keys must be tried to achieve success. In most networking system, algorithms are known to all so in this case, brute-force attack will impossible if the algorithm uses large number of keys. At present the fastest super computer is Tianhe-2 having speeded 33.86 petaflops i.e.,  $33.86 \times 10^{15}$  floating point operations per second. Let us consider each trial requires 2000 FLOPS to complete one check. So number of trials complete per second is:  $16.93 \times 10^{12}$ . The number of second in a year is:  $365 \times 24 \times 60 \times 60 = 3153600$  sec.

Now from the above key space the formula for break the keys is  $2^{3x/2} / (16.93 \times 10^{12} \times 3153600) = Y$ . So if  $k$  increase then  $Y$  increases. The following table and graphs shows the average time required for exhaustive key search [3].

**Table4.** Exhaustive Search analysis

Symmetric key size (x bits)	No. of Trials in standard algorithms( $2^x$ )	Time Re-quired(in years) at $16.93 \times 10^{12}$ Decryption/s in standard algorithms	No. of Trails in our proposed technique ( $2^{(3x/2)}$ )	Time Re-quired(years) at $16.93 \times 10^{12}$ Decryption/s in proposed technique
56	$2^{56}$	0.001349	$2^{84}$	362289
64	$2^{64}$	0.34550	$2^{96}$	1483938
128	$2^{128}$	$6.3734 \times 10^{18}$	$2^{192}$	$1.1775 \times 10^{38}$
166	$2^{166}$	$1.7519 \times 10^{30}$	$2^{249}$	$1.6943 \times 10^{55}$

192	$2^{192}$	$1.1756 \times 10^{38}$	$2^{288}$	$9.3148 \times 10^{66}$
256	$2^{256}$	$2.1687 \times 10^{57}$	$2^{384}$	$7.3799 \times 10^{95}$
300	$2^{300}$	$3.8153 \times 10^{70}$	$2^{450}$	$5.4454 \times 10^{115}$



**Fig3.** 3D graph of exhaustive key search

**OBSERVATIONS:** - From the above table it is seen that with respect to number of trials our proposed technique provides good result than any standard algorithms (like DES, Triple DES, AES etc) with same key size. The x-axis of the graph represents key size in bits. The above table and graph also shows that our proposed technique provides good result for decryption than any standard algorithms (like DES, Triple DES, AES etc) with fixed decryption rate. So, it difficult for attacker to decrypt any cipher text using assumed key. Thus overall result of our technique is good with respect to any standard algorithms in brute force attack.

**DICTIONARY ATTACKS:** -

Passwords found in any on-line or available list of words may be uncovered using dictionary attack by an attacker who tries all words in this list. The traditional dictionaries are not only used to find password but also on-line dictionaries of words from foreign languages, or on specialized topics such as music, film, sports etc. are used. For repeated use of these words in encryption process an adversary may create, an “encrypted” (hashed) list of dictionary or high-probability passwords. This dictionary may be used by attacker in guessing right encryption key for decryption. Dictionary attacks are more efficient than a brute force attack because it cannot try nearly as many combinations and if the key is not contained in the dictionary, it will never successfully find it.

In our proposed methodology, we have used random number generation functions, concept of matrix and fuzzy function and as a result the session key generated in this way not only contains English words or variations or phrases but also contains different ascii characters, numbers, and special characters. This would exhaust attacker’s dictionary without a positive match.

**RANDOMNESS TEST & ENTROPY TEST OF SESSION KEY:** - In our technique the session key is generated from symmetric key using fuzzy logic. Now to test the randomness of session key we use some standard techniques such as frequency test [14], entropy [15].

**FREQUENCY TEST:** -The frequency test is the most basic test for randomness checking. The purpose of this test is to determine whether the number of 1’s and 0’s in a sequence is approximately the same as would be expected for a truly random sequence.

**Mathematical Structure of the Test:**

*Frequency (n)*, where n is the length of bit string.

$\mathcal{E}$ : the sequence of bits which are generated by RNG or PRNG.

$S_{obs}$ : the absolute value of the sum of the  $X_i$  (where  $X_i = 2\mathcal{E}_i - 1$ ) is the sequence divided by the square root of the length of the sequence.

- 1) Conversion to  $\pm 1$ : The zeros and ones of the input sequences ( $\mathcal{E}$ ) are converted to values of -1 and +1 and are added together to produce  $S_n = X_1 + X_2 + \dots + X_n$ , where  $X_i = 2\mathcal{E}_i - 1$ .
- 2) Compute the test static  $S_{obs} = \text{ABS}(S_n)/\sqrt{n}$ .

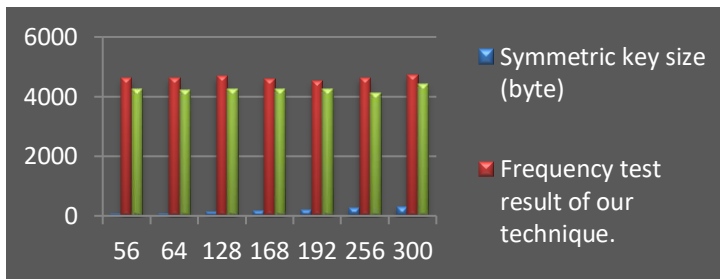
3) Compute P-value=  $erfc(S_{obs}/\sqrt{2})$ .

4) If P-value $\geq 0.01$  then the conclusion is that the sequence is random and if P-value $< 0.01$  then the sequence is not random.

The following table shows the details.

**Table5.**Table for Frequency test result

Symmetric key size (bits)	Frequency test result of our technique.	Frequency test result of PRNG()
56	4598.256	4272.772
64	4625.147	4310.446
128	4662.584	4336.617
166	4579.128	4270.683
192	4519.967	4270.656
256	4633.422	4323.351
300	4722.322	4423.356



**Fig4.**Graph of frequency test of above table

**OBSERVATIONS:** - NIST SP 800-22 specifies that the randomness test must follow the three characteristics such as Uniformity, Scalability and Consistency.

In case of uniformity and scalability, the occurrence of a zero or one is equally likely that is the probability of occurrence of zero or one is half. The above table of frequency test result shows uniformity and scalability of our technique.

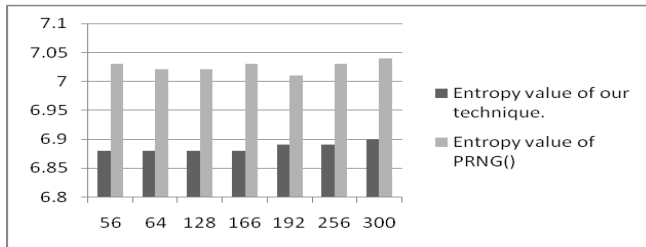
In case of consistency, we can say that the seed value from which we can generate the session key is symmetric key. For cryptographic applications, the symmetric key must be secure. The session key is generated by using a random key matrix and a symmetric key. Now if the key matrix is unknown or may change time to time and if the symmetric key is secured then the next output bit in the sequence should be unpredictable in spite of any knowledge of previous bits in the sequence.

It should not be feasible to determine the symmetric key from the knowledge of any generated values. There is no correlation between symmetric key and generated values. Thus our technique proves the forward and backward unpredictability. Furthermore, from the above table and graph it is seen that our proposed technique provides more randomness than PRNG () which is standard technique.

**EXPERIMENT ON ENTROPY VALUE -:** Here we describe a comparative study between our technique and standard technique, PRNG () with session key and symmetric key.

**Table6.** Entropy value

Sym-metric key size (bits)	Entropy value of our technique.	Entropy value of PRNG()
56	6.88	7.03
64	6.88	7.02
128	6.88	7.02
166	6.88	7.03
192	6.89	7.01
256	6.89	7.03
300	6.90	7.04



**Fig5.2D** Graph of Entropy value of above table

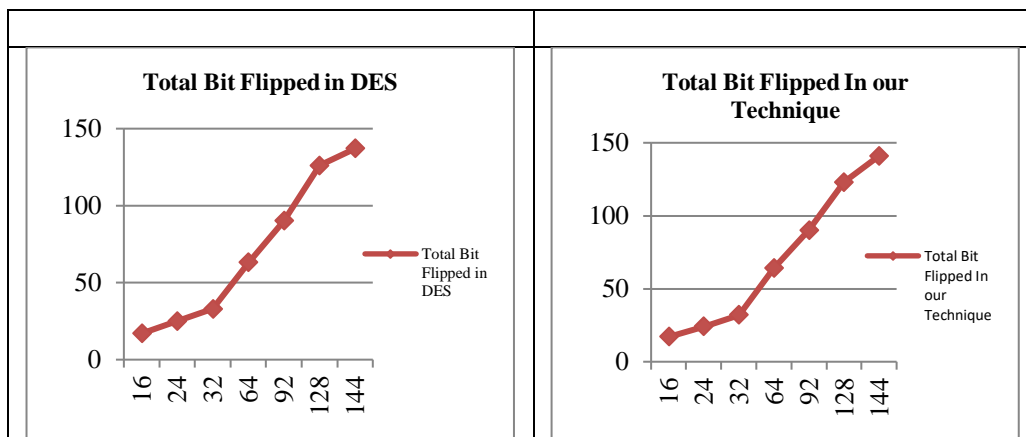
**OBSERVATIONS:** - In cryptography, a cryptosystem is said to be semantically secure if it is computationally impossible for an attacker to extract any information about the plain text from cipher text and its length. Entropy can be defined as randomness or unpredictability of information contained in a message. This randomness breaks the structure of plain text. Entropic security in encryption is similar to semantic security when data have highly entropic distribution. Plain text entropy value is zero. Now from the comparative study of entropy value between our technique and PRNG (), it is seen that the entropy value of our technique is near to the result of PRNG (). The x-axis shows the key length. Thus from the definition of entropic security we say that it is very hard to predict plain text from cipher text if we use our technique to generate session key and the use of this session key and symmetric key in encryption provides robustness.

**COMPARATIVE STUDY ON AVALENCHE EFFECT:-**

Here a comparative study between our technique and DES on avalanche effect [3], [16] with fixed key is described below with a table and graph.

**Table7.** Table for Avalanche effect with fixed key

Text Size (byte)	Total bit flipped in DES	Total bit flipped in our Technique
17	17	17
24	25	24
32	33	32
64	63	64
92	90	90
128	126	123
144	137	141



**Fig6.** Graph of Avalanche effect with fixed key for above table

**OBSERVATIONS:** - A desirable property of any encryption algorithm is that a small change in either the plaintext or the key should produce a significant change in the cipher text. In particular, one bit

change in the plaintext or one bit in the key should produce a change in many bits of the cipher text. Thus avalanche [3] quantifies the effect on the cipher text when one bit change in plaintext. An encryption algorithm that doesn't provide the avalanche effect can lead to an easy statistical analysis that is if the change of one bit from the input leads to the change of only one bit of the output, then it's easy to guess. Above table and graph provides comparative study between DES and our technique. In the graph x-axis represent text size. This study tells that total number of bit flipped in our encryption technique is more than DES. Here we use fixed size key. Thus our technique (using fixed key) provides good result than any standard algorithm (like DES). So, our proposed scheme satisfies the desirable property for encryption algorithm.

**ANALYSIS OF OUR ENCRYPTION TECHNIQUE:** - Cryptanalysis is the study of cipher text, ciphers and cryptosystems. The aim of cryptanalysis is to understand how they work and finding and improving the techniques for defeating or weakening them. There are different types of cryptanalysis attacks such as Cipher text Only Attack, Chosen plain text Attack, Known Plaintext Attack, Chosen cipher text Attack, Breaking an encryption algorithm is basically the finding of the key to the access the encrypted data in plain text. For symmetric key encryption, breaking the algorithm usually means trying to determine the key used to encrypt the text. For a public key encryption, breaking the algorithm usually means acquiring the shared secret information between two recipients. The robustness of an encryption technique is depends on non linearity in cipher text. In our paper we use circular left shift operation and a non linear function to provide non linearity in cipher text. As a result our technique is able to protect any types of cryptanalysis attack. The following graph shows the robustness of our protection mechanism.

<b>Message: Happy New Year. GOD Bless You.</b>		<b>Symmetric Key: abc1981504 and Session Key: #@16PaD03M</b>	
Encryption with simple xor operation		Encryption with our proposed algorithm	
<p><b>Comparative Analysis between plain text and cipher text generated by XOR .</b></p>		<p><b>Comparative Analysis between plain text and cipher text generated by proposed algorithm</b></p>	

**Fig7.** Analysis of Encryption Technique

**OBSERVATIONS:** - Non linearity is a main theme in any encryption technique. From the above fig.6 it is seen that our technique provides more non linearity in cipher text than simple XOR operation. If we consider any point (x, y) and (a, b) in the plaintext and Cipher\_Proposed respectively of above graph then any periodic gap is not exists between points in the graph i.e., there is no relationship between two graphs. So it is hard to guess plain text or encryption key from cipher text. Thus our encryption scheme is robust as well as it may protect any types of cryptanalysis like known plain text attack, chosen cipher text attack etc. From above Theorem1, it is also seen that this technique satisfies the condition of perfect security because cipher text and plain text are independent.

COMPARATIVE DISCUSSION OF OUR PROPOSED TECHNIQUE: - In this section the functionality of our scheme is done by comparing our proposed technology with different standard cryptographic algorithms, different existing schemes [15, 17, 18, 19, 20, 21].

The following tables show comparison among different standard algorithms and our proposed algorithm.

**Table8.** Comparisons among proposed technique & standard algorithms

<b>Algorithms</b>	<b>Important Features</b>	<b>Important features of our proposed algorithm</b>
IDEA	<ul style="list-style-type: none"> <li>i) IDEA encrypts 64-bit plaintext to 64-bit cipher text blocks, using a 128-bit input key.</li> <li>ii) It uses both confusion and diffusion technique.</li> <li>iii) A dominant design concept in IDEA is mixing operations from three different algebraic groups of <math>2^n</math> elements.</li> <li>iv) The security of IDEA currently seems that it is bounded only by the weaknesses arising from the relatively small (compared to its key length) block length of 64 bits.</li> </ul>	<ul style="list-style-type: none"> <li>i)Our technique encrypts n-bit plaintext to n-bit cipher text, using m-bit input key.</li> <li>ii) The main design concept of our technique (a) symmetric key generation using the concept of linear congruence. (b) Session key generation using approximation algorithm. (c)Circular left shift is used to produce non linearity in encryption process.</li> </ul>
RC5	<ul style="list-style-type: none"> <li>i) The RC5 block cipher has a word-oriented architecture for variable word sizes <math>w = 16, 32, \text{ or } 64</math> bits.</li> <li>ii) The number of rounds <math>r</math> and the key byte-length <math>b</math> are variable.</li> <li>iii) For encryption, there are two steps in each round, (a) bit-wise XOR operation, (b) circular left shift. (c) Addition with the next sub key.</li> </ul>	<ul style="list-style-type: none"> <li>i)Our proposed scheme is stream cipher based. Here two keys are used for encryption/decryption.</li> <li>ii) Key length is variable.</li> <li>iii) For encryption, there are two steps-(a) bit-wise XOR operation (b) Circular left shift with a linear function. It provides number of times CLS occurs.</li> </ul>
BLOWFISH	<ul style="list-style-type: none"> <li>i)This technique is based on stream cipher. It uses addition, XOR operation for encryption.</li> <li>ii)It has a variable key length up to a maximum of 448 bits long which ensures security.</li> <li>iii) Blowfish suits applications where the key remains constant for a long time and it is not suitable for packet switching.</li> </ul>	<ul style="list-style-type: none"> <li>i)Our scheme is also based on stream cipher. It uses XOR, CLS operations to impose more non linearity in cipher text.</li> <li>ii) The use of double keys and one of this key is changeable by nature which provides robustness in our technique.</li> <li>iii)Suitable for packet switching.</li> </ul>
DES	<ul style="list-style-type: none"> <li>i) Linear cryptanalysis provides the most powerful attack on DES to date where enormous number of known plain text pairs is feasible.</li> <li>ii) Differential cryptanalysis is one of the most general cryptanalytic tools to date against modern iterated block ciphers, including DES. It is primarily a chosen-plaintext attack.</li> <li>iii) Storage complexity, both linear</li> </ul>	<ul style="list-style-type: none"> <li>i)Our algorithm is based on stream cipher with two keys one is session key which is changeable in nature. So it protects linear cryptanalysis as well as differential cryptanalysis.</li> <li>ii) Our algorithm takes negligible storage for linear and differential cryptanalysis.</li> <li>iii) Our algorithm is secure with</li> </ul>



	<p>and differential cryptanalysis requires only negligible storage.</p> <p>iv) Due to its short key size, the DES algorithm is now considered insecure and should not be used.</p> <p>However, a strengthened version of DES called Triple-DES is used.</p>	<p>respect to key size, because we have used two keys with variable length.</p>
Triple-DES with Three keys	<p>i) Triple-DES counters to the meet-in-the-middle attack by using three stages of encryption with three keys.</p> <p>ii) Tuchman proposed a triple encryption method that uses only two keys. The function follows an Encrypt-Decrypt-Encrypt sequence.  <math>C = E(K_1, D(K_2, E(K_1, P)))</math> and  <math>P = D(K_1, E(K_2, D(K_1, C)))</math></p> <p>iii) There is no cryptographic significance in 2<sup>nd</sup> stage decryption. Its only advantage is that it allows users to decrypt information encrypted by users of single DES.</p> <p>iv) There is no practical cryptanalytic attack on 3DES. This method is an improvement over the chosen plain text approach but requires more effort. This attack is based on observation that if the value of 1<sup>st</sup> phase encryption and final cipher text is known then the problem reduces to double DES.</p>	<p>i) This article proposed a method that counters meet-in-the-middle attack by using two different keys with variable times of CLS.</p> <p>ii) This technique has cryptographic importance in wireless network; it uses two keys such as symmetric key and session key which is generated using fuzzy logic. It also provides strong authentication mechanisms.</p> <p>iii) It is very hard to anticipate the two keys if plaintext-cipher text pair is known.</p>

The following table provides the pertinence of our methodology compared to other existing techniques.

**Table 9.** Comparison among some existing schemes and our proposed scheme

Schemes → Security Properties ↓	Ref. [15]	Ref. [17]	Ref. [18]	Ref. [19]	Ref. [20]	Ref. [21]	Proposed technique
Confidentiality	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Integrity	Yes	No	No	Yes	Yes	Yes	Yes
Authenticity (message authentication)	Yes	Yes	No	No	No	No	Yes (using symmetric key & session key).
Freshness Protection	No	No	No	No	No	No	Yes
Privacy Protection	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Man-in-middle attack	Yes	No	No	No	No	No	Yes
Tenability	No	No	No	No	No	No	Yes
Vulnerability	Yes	Yes	No	No	No	Yes	Yes
Impersonation attack	No	Yes	Yes	No	No	No	Yes
Cryptanalysis (linear and differential)	Yes	No	No	No	No	No	Yes

Session key establishment	No	No	No	No	No	No	Yes
Information-leakage attack	Yes	No	Yes	Yes	No	Yes	Yes

## 4 Concluding Remarks

We have presented a key generation technique and an encryption technique based on symmetric key and session key for secure data transmission in wireless network. This session key is generated from symmetric key using some tools such as recurrence relation, fuzzy logic, and random matrix. Here receiver decrypts the cipher text using his or her symmetric key and session key. Our technique also provides the proof of identities which enrich the robustness as well as beauty of our proposed scheme. Thus our technique provides two contributions on symmetric key encryption. Firstly, a new approach for extracting session key from secured symmetric key and a random matrix. This random matrix provides randomness of our session key. Secondly, the random matrix is generated from random numbers and this random numbers are generated from recurrence relation from discrete mathematics. The use of recurrence relation is a new approach in random number generation. It provides variable number of random numbers depending on initial value and context values and total numbers of random numbers depend on user. Thirdly, the encryption technique with two keys i.e., two times encryption with session key and symmetric key and circular left shift operation on partial encrypted form provides robustness of our technique. At last we have included an authentication mechanism in our technique. Comparative statistical tests like entropy value and frequency test etc between proposed technique and standard technique proves the sturdier of our key. Lastly, exhaustive key search analysis shows the acceptability of our technique. To the best of our knowledge our proposed technique is the simplest encryption technique with symmetric key, session key with authentication mechanisms. It is practically having minimal computational overhead during encryption and decryption.

Conflict of Interest: The authors declare that they have no conflict of interest.

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